Lecturer 6, 7, 8, 9

Radio Communication Systems

Outline

- Introduction
- Types of Digital Modulation
  - Frequency Shift Keying FSK
    - MSK Minimum Shift Keying
  - Amplitude Shift Keying ASK
  - Phase Shift Keying PSK
- M-ary PSK Encoding
  - Quadrature QPSK
  - 8-PSK
- QAM: (8-QAM)
- Carrier Recovery Circuits

Digital Radio

- **Why Digital ?**
  - Ease of processing,
  - Ease of multiplexing, and
  - Noise immunity.
- **All Digital Communications**
  - Transmission, reception and processing of information.
- **Increasing of Information Capacity**
  - No of independent symbols that can be carried through system in a given time.

Information Capacity

- **1928 Hartley introduces useful rule:**
  - Capacity C is proportional to both the bandwidth B and the time T :

$$C \sim B\,T$$

- **1948 Shannon published a limit for C :**

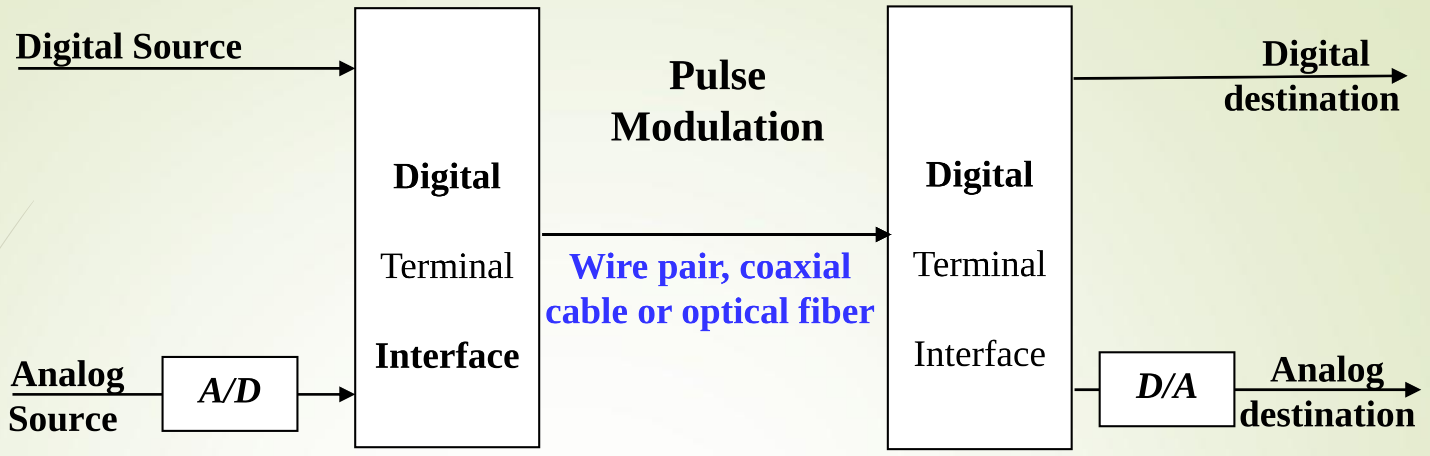
$$C \leq B \log_2\left(1 + \frac{S}{N}\right) = 3.32\,B \log_{10}\left(1 + \frac{S}{N}\right)$$

- $S/N = 1000\ (30\ \mathrm{dB}), B = 2.7\mathrm{kHz},\ C$:

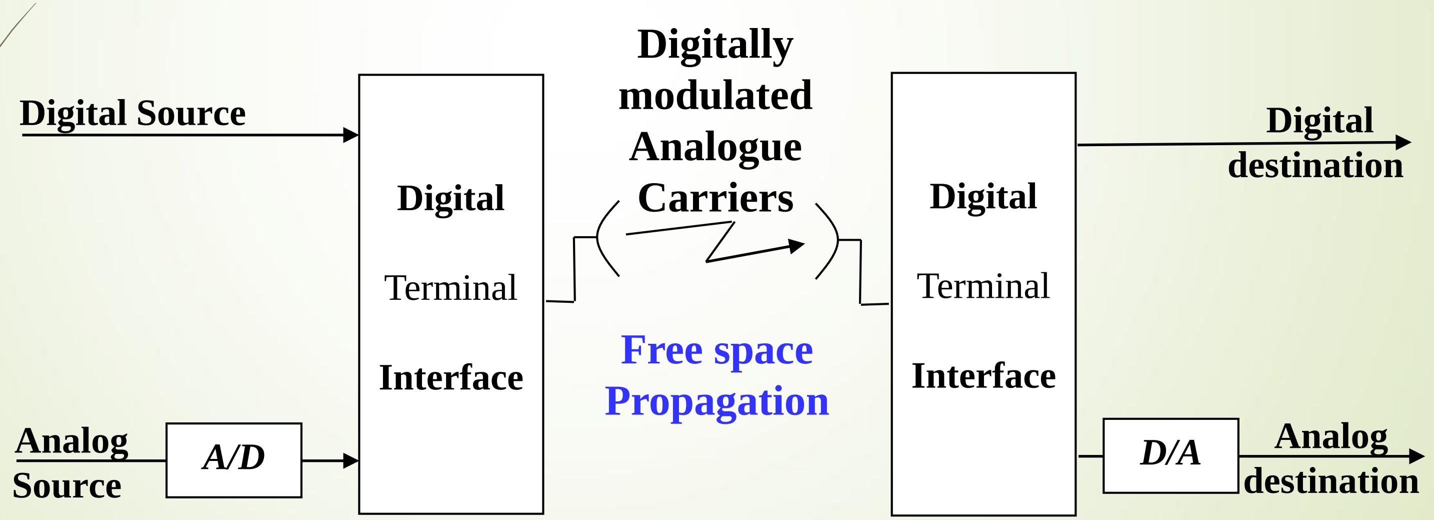
$$C \leq 2700 \log_2(1 + 1000) \leq 26.9\ kbps$$

Limit Misunderstood

- Above example may be true, but it cannot be done with a binary system.
- To achieve 26.9 kbps through 2.7 kHz channel, each symbol must contain more than one bit of information.
- So, to achieve Shannon limit, digital transmission systems that have more than two output conditions (symbols) must be used.



(a) Baseband Transmission



(b) Digital Radio Transmission

Types of Modulation

- تعديل إزاحة السعة Amplitude Shift Keying ASK.
- تعديل إزاحة التردد Frequency Shift Keying FSK.
  - تعديل الإزاحة الدنيا Minimum Shift Keying MSK
  - تعديل الإزاحة الدنيا الجاوسي Gaussian Minimum Shift Keying GMSK.
- تعديل إزاحة الطور Phase Shift Keying PSK.
  - تعديل إزاحة الطور الثنائي Binary Phase Shift Keying BPSK.
  - تعديل إزاحة الطور التفاضلي Differential Phase Shift Keying DPSK.
- تعديل إزاحة الطور متعدد المستويات M-ary Phase Shift Keying.
  - تعديل إزاحة الطور التعامدي Quadrature Phase Shift Keying QPSK.
  - تعديل إزاحة الطور الثماني Eight Levels Phase Shift Keying 8PSK
- تعديل السعة التعامدي Quadrature Amplitude Modulation QAM.

FSK

Frequency Shift Keying

FSK Transmitter Signal

- Simple, low performance.
- Constant envelope angle modulation.

$$v_{FSK}(t) = V_c cos\left[\left(\omega_c + f_m(t)\frac{\Delta\omega}{2}\right)t\right]$$

  - $f_m(t)$ binary digital modulating signal
  - V_c, ω_c, carrier amplitude, frequency
  - Carrier frequency shifts between $\omega_c \pm \Delta\omega/2$
  - Shift rate equals the input bit rate f_b b/s.

FSK Transmitter

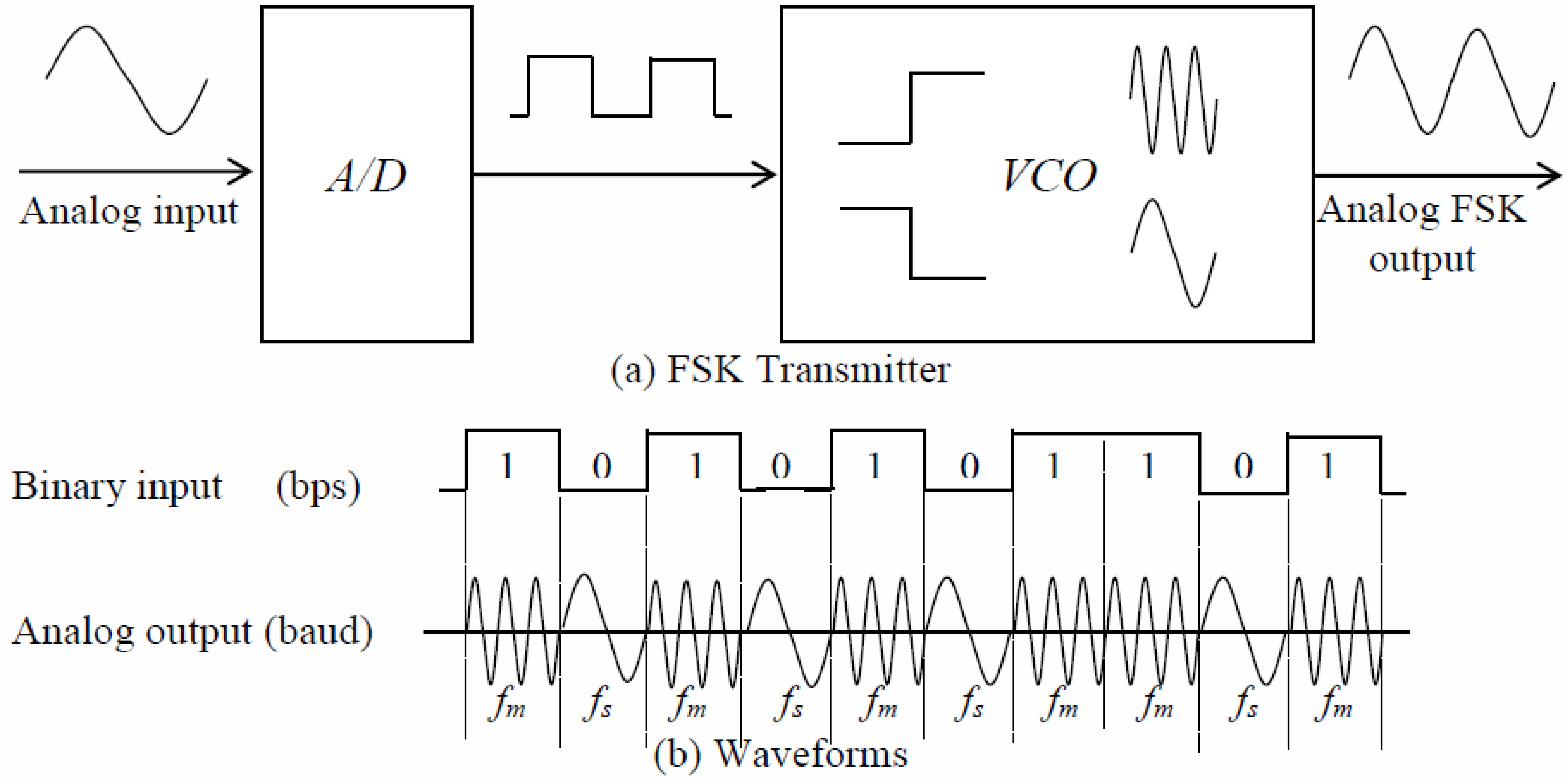
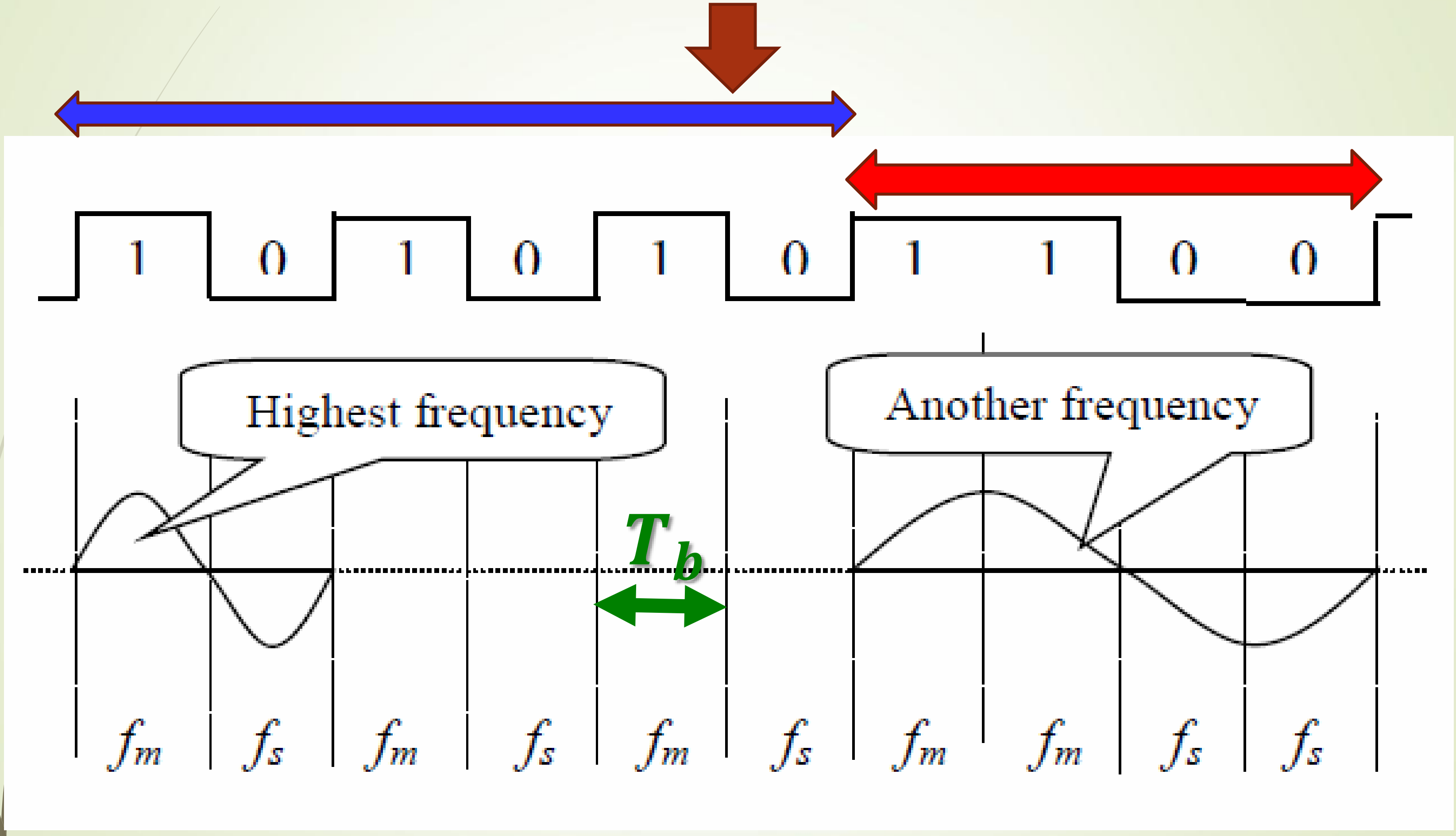


Fig 2.2 Binary FSK Modulator

Bit and Baud Rates

- **Bit rate**, in bits per second,
  - Is the rate of change at the input to the modulator.
- **Baud rate, in symbol per sec**
  - Is the rate of change at the output of the modulator and
  - Is equal to the reciprocal of the time of one output signaling element (termed as symbol).
- So, baud is the line speed in symbols per second.

Possible frequencies



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Highest Modulating Frequency

- If bit width is T_b, bit rate will be $f_b = \frac{1}{T_b}$
- Fastest rate occurs when input is a series of alternating 1's and 0's:
- If fundamental frequency is considered, highest modulating frequency is one-half the input bit rate.

$$f_m = \frac{f_b}{2}$$

Modulation Index of FSK

- Peak frequency deviation Δf is one half the difference between f_m and f_s:

$$\Delta f = \frac{f_m - f_s}{2}$$

- Formula for modulation index used in FM is also valid for binary FSK as:

$$MI = \frac{\Delta f}{f_m} = \frac{\frac{f_m - f_s}{2}}{\frac{f_b}{2}} = \frac{f_m - f_s}{f_b}$$

- MI is kept below 1.0 for narrow band FM.
- BW is determined from Bessel functions table.
- MI 0.5 and 1.0, either two or three sets of significant side frequencies are generated.
- Thus, minimum BW is two or three times the bit rate.

Bandwidth of Binary FSK

- BW for FSK signal is given by Carson's rule in terms of the frequency deviation and the bandwidth of the digital modulation

$$BW_{FSK} = 2(\Delta f + B)$$

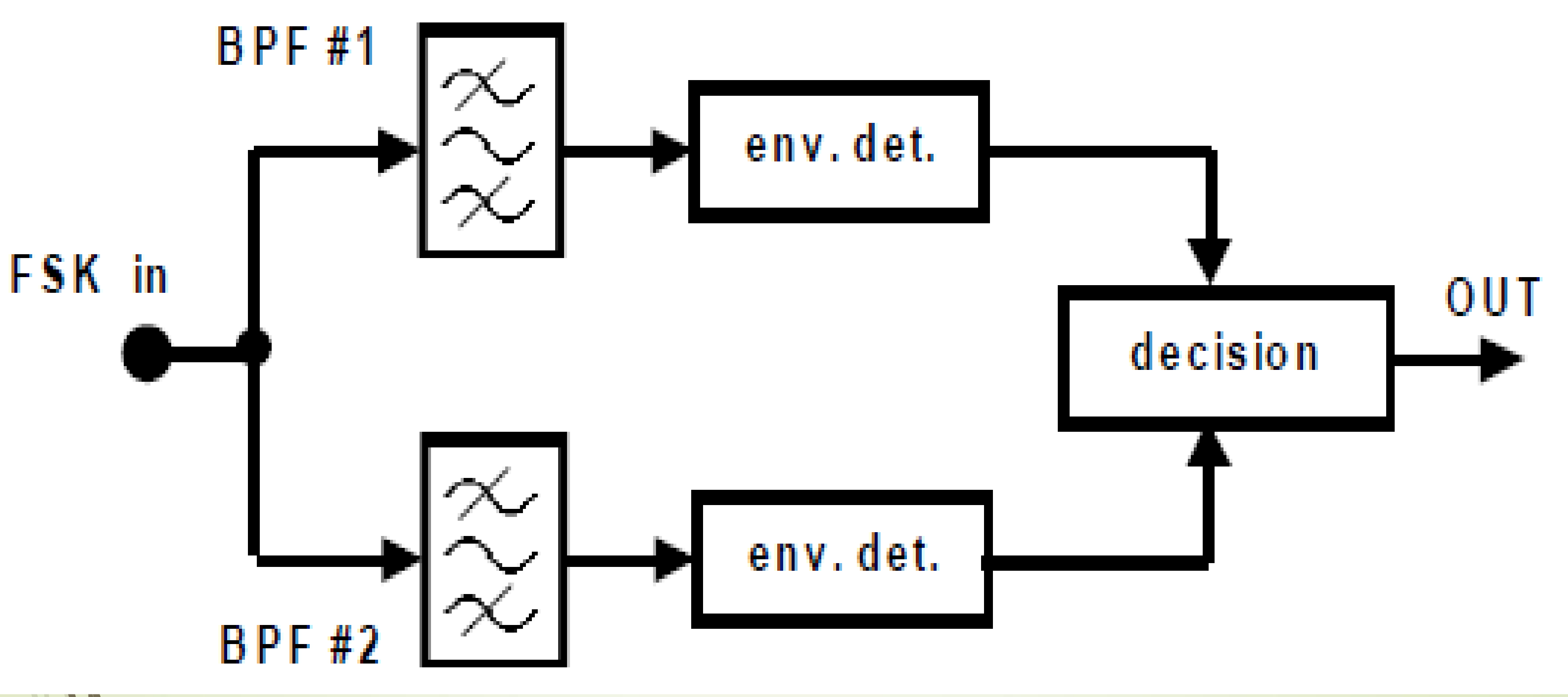
- For alternating 1 and 0, the bandwidth equals the bit rate $B = R$:

$$BW_{FSK} = 2(\Delta f + R)$$

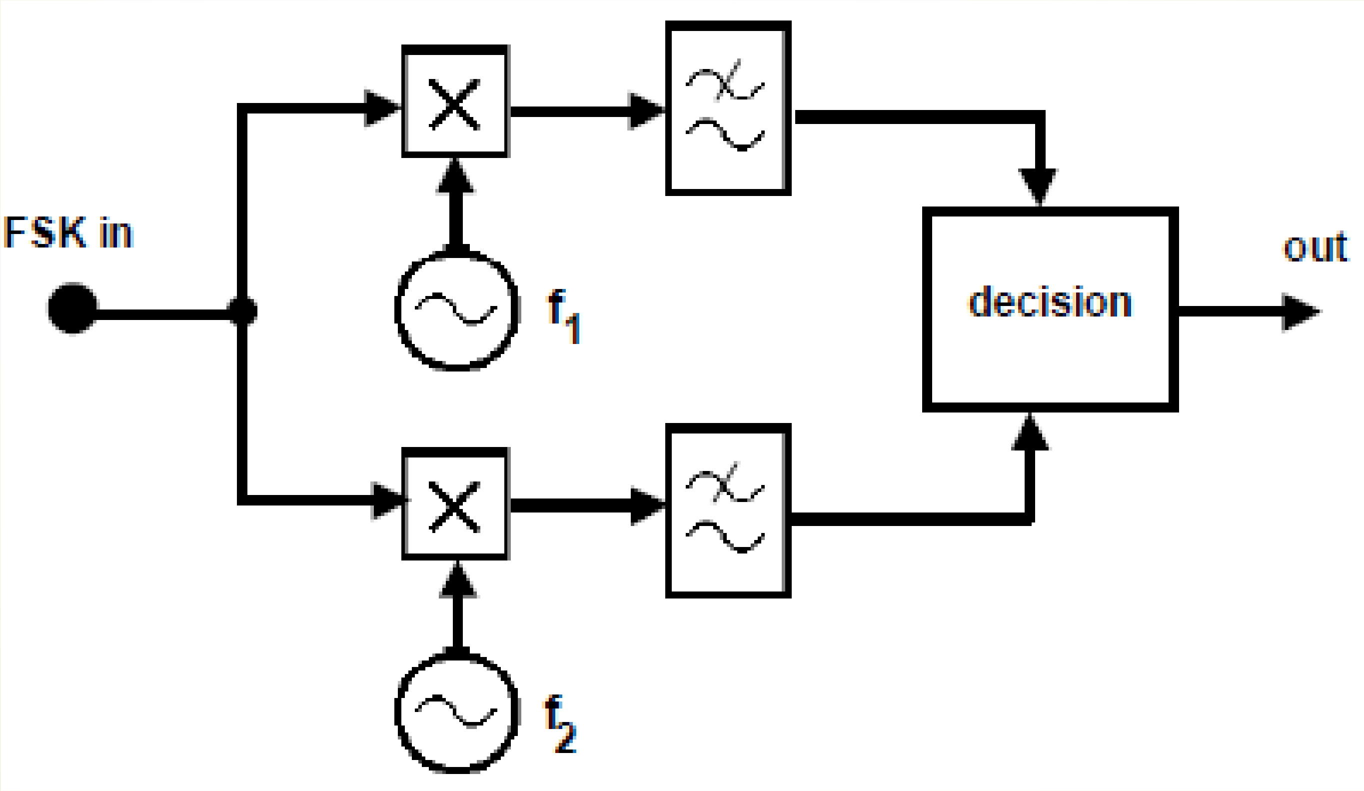
Receiver Binary FSK

- Noncoherent Detection:
  - We do not have knowledge of the carrier.
  - Signal coming is divided into two BPF and envelope detectors.
  - Finally, binary restoration circuit.
- Coherent detection:
  - We need a complete knowledge of the exact carrier frequency on reception.
  - Received signal is applied into two multipliers, at f1 and f0, then to LPF.
  - Finally binary restoration circuit.

FSK Noncoherent Detector



FSK
Synchronous Detector



Applications of FSK

- Binary FSK has a poorer error performance than PSK or QAM.
- Its use is restricted to low-performance, low-cost, asynchronous data **modems** that are used for **data communication** over analogue, voice band **telephone lines.**

Bell 103-type FSK Modem

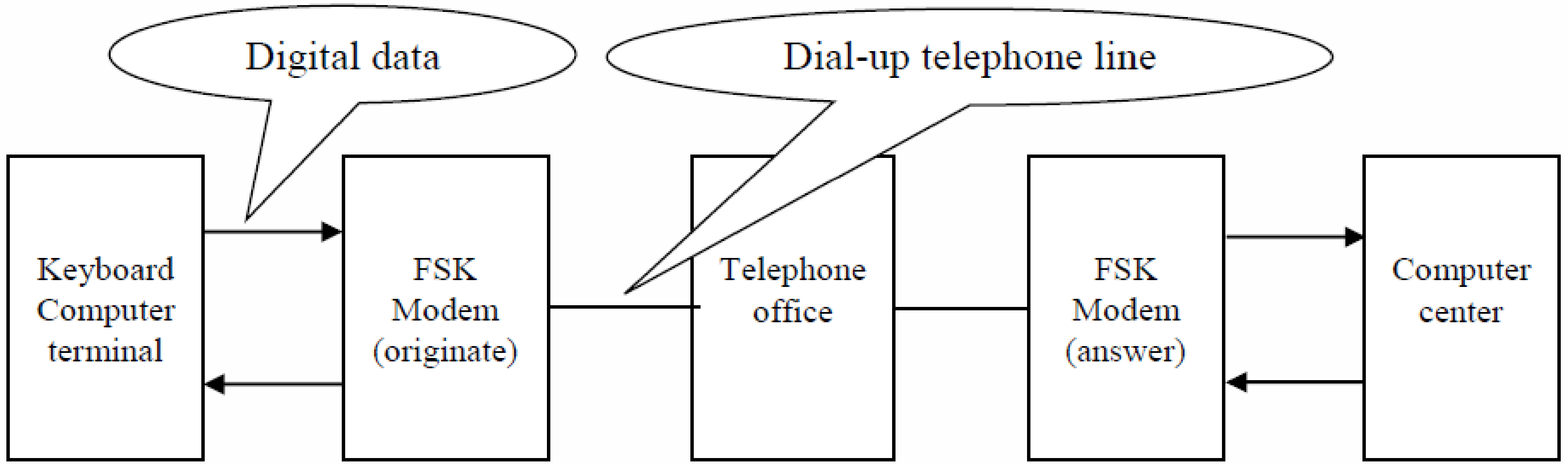


Table 2.1 Mark and Space Frequencies for the Bell Type 103 Modem

	Data	Originate Modem	Answer Modem
Transmit frequencies	Mark (binary 1)	$f_1 = 1270$ Hz	$f_1 = 2225$ Hz
	Space (binary 0)	$f_2 = 1070$ Hz	$f_2 = 2025$ Hz
Receive frequencies	Mark (binary 1)	$f_1 = 2225$ Hz	$f_1 = 1270$ Hz
	Space (binary 0)	$f_2 = 2025$ Hz	$f_2 = 1070$ Hz

Bell 103-type FSK Modem

- Keyboard-type computer terminals are often used for communication with a remote computer via dial-up telephone lines.
- Dial-up means that the computer terminal user calls the computer facility on a telephone and uses the telephone connection for data communication.
- Modem (modulator and demodulator) is connected to the phone line at each end as shown
- Two FSK frequency bands are used (one around 1 kHz and another around 2 kHz) so that it is possible to talk and listen simultaneously (full-duplex).
- The standard mark and space frequencies are shown in Table where the peak to peak deviation is $2\Delta F = 200$ Hz

MSK

Minimum Shift Keying

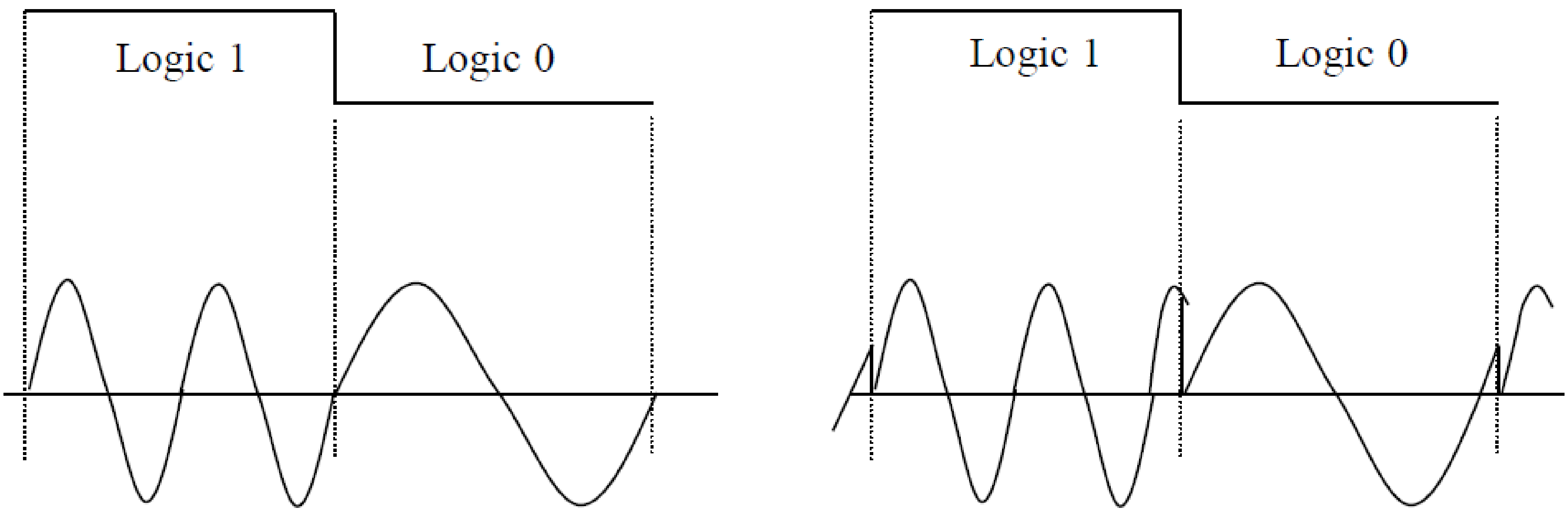
Minimum Shift Keying

- MSK is a continuous phase FSK keying (CPFSK).
- MSK is FSK except mark and space frequencies are synchronized with input binary rate.
- Synchronous means precise time relationship.
- Mark and space frequencies are separated from center frequency by odd multiple of one-half f_b

$$f_m \; and \; f_s = n\frac{f_b}{2}$$

- MSK has a better bit error performance than FSK for a given signal to noise ratio.
- MSK has less bandwidth than FSK
- However, it requires synchronizing circuits and is therefore more expensive to implement.

MSK versus FSK



(a) Continuous Phase MSK

(b) Non-continuous FSK

Fig.2.8 Comparison of the Phase Continuity between MSK and FSK

ASK

Amplitude Shift Keying

Amplitude Shift Keying

- In ASK, amplitude of carrier switches between; zero (Off state) and some amplitude (On state)
- Such systems are termed on-off-keyed systems OOK.
- Spectrum of OOK depend on the particular binary sequence to be transmitted. However, the amplitude modulated OOK is the DSB.SC given by:

$$f_{OOK}(t) = f_{ASK}(t) = A\,f(t)\cos\omega_c t$$

- Spectrum of OOK signal is given as:

$$F_{OOK}(\omega) = F_{ASK}(\omega) = \frac{A}{2}\left[F(\omega-\omega_c) + F(\omega+\omega_c)\right]$$

OOK Waveforms

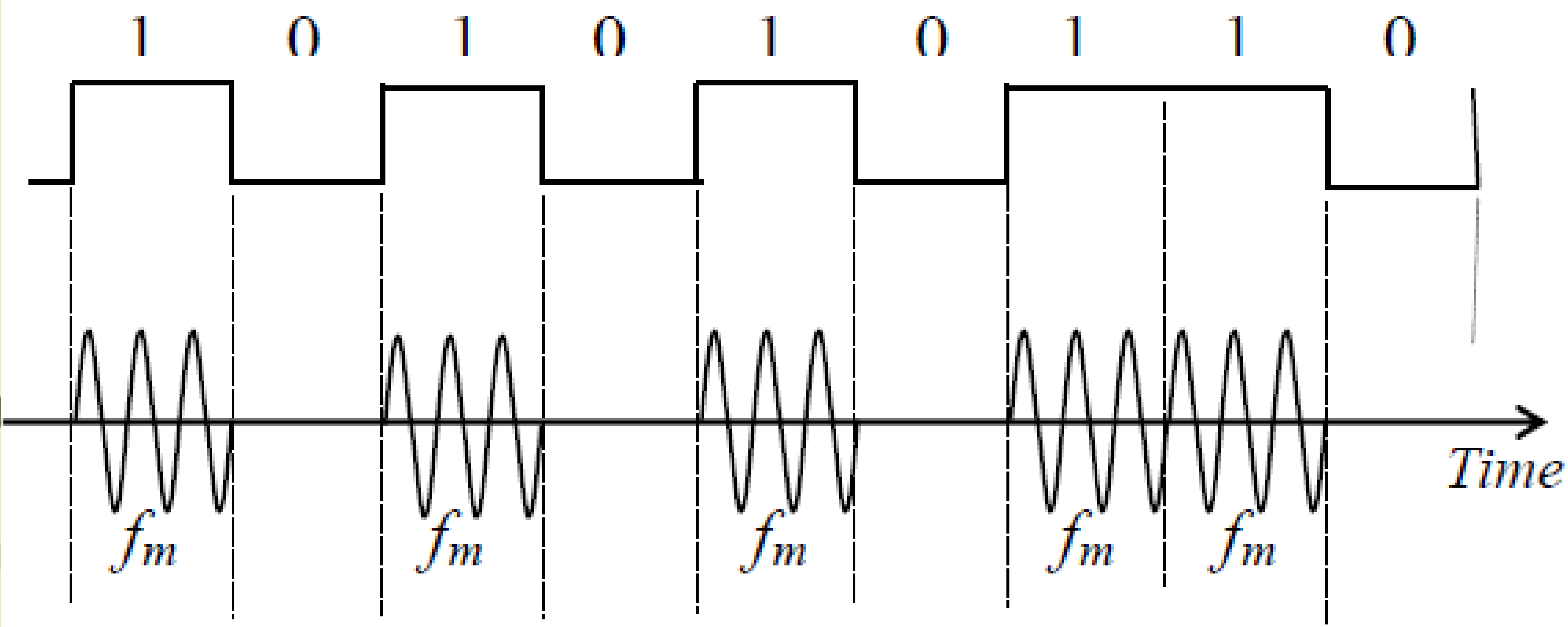


Fig.2.9 ASK or OOK Signal

Spectrum of OOK

- Assume the digital signal *f(t)* is rectangular pulse (special case of binary in which all symbols are 0 except for one 1).
- For a pulse of amplitude *A* and duration *T*, the spectrum of OOK modulator is given by:

$$F_{OOK}(\omega) = \frac{AT}{2}\left[\frac{\sin(\omega-\omega_c)T/2}{(\omega-\omega_c)T/2} + \frac{\sin(\omega+\omega_c)T/2}{(\omega+\omega_c)T/2}\right] = \frac{AT}{2}\left[Sa\left\{\frac{(\omega-\omega_c)T}{2}\right\} + Sa\left\{\frac{(\omega+\omega_c)T}{2}\right\}\right]$$

- For alternating 1's and 0's, spectrum is (sin x) /x.
- So, spectrum of pulse of width *T* and period 2*T* which is translated to frequency f_c as in Fig.2.10

Spectrum of Periodic OOK

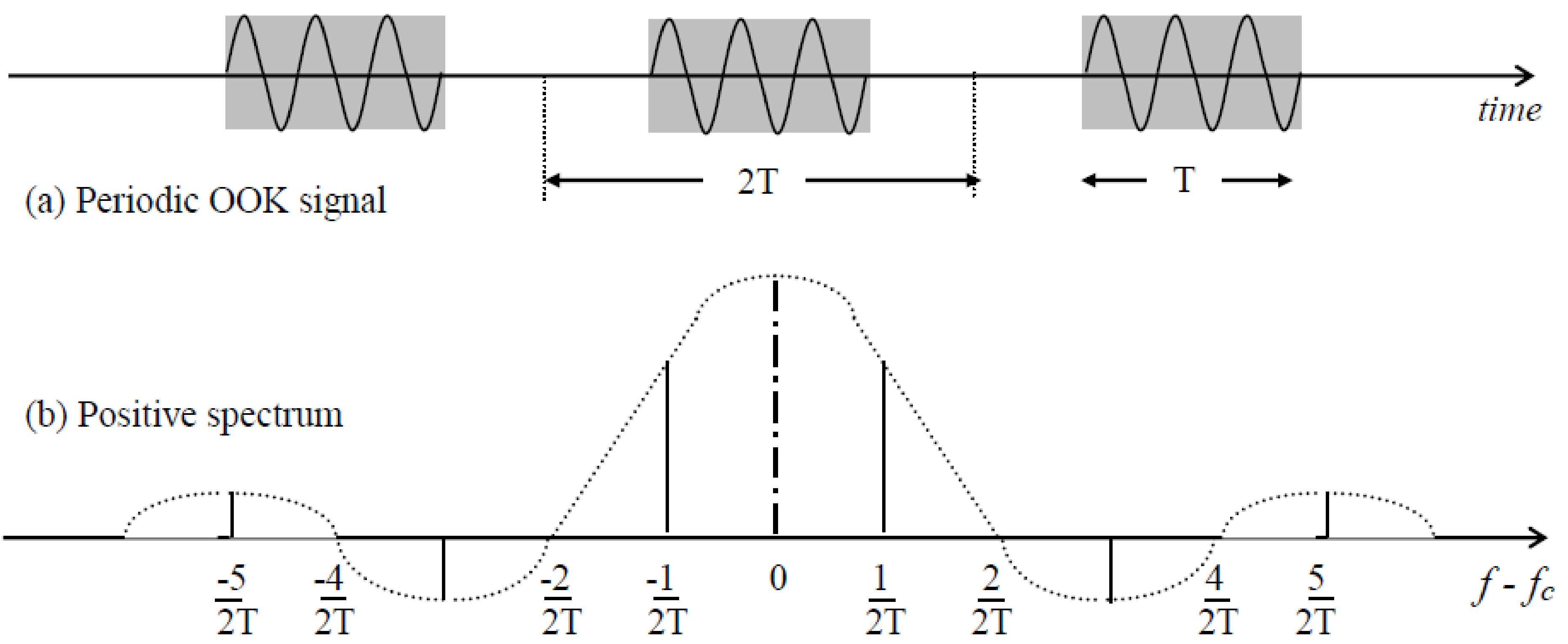


Fig.2.10 Spectrum of Periodic OOK Signal

PSK

Phase Shift Keying

Phase Shift Keying

- PSK is similar to phase modulation PM except that its input gives rise to a limited number of output phases.
- With binary BPSK two output phases are possible for a single carrier frequency. One phase represents a logic 1 and the other represents a logic 0.
- With carrier amplitude V_c and frequency ω_c PSK voltage for binary digital modulating signal *f(t)* is:

$$v(t) = V_c f(t) \sin \omega_c t = \begin{cases} +V_c \sin \omega_c t & if \quad f(t) = +1 \\ -V_c \sin \omega_c t & if \quad f(t) = -1 \end{cases}$$

- So, the carrier amplitude remains constant, whereas its phase shifts by 180^o.
- Recall, carrier phase shift rate equals input bit rate.

BPSK Waveforms

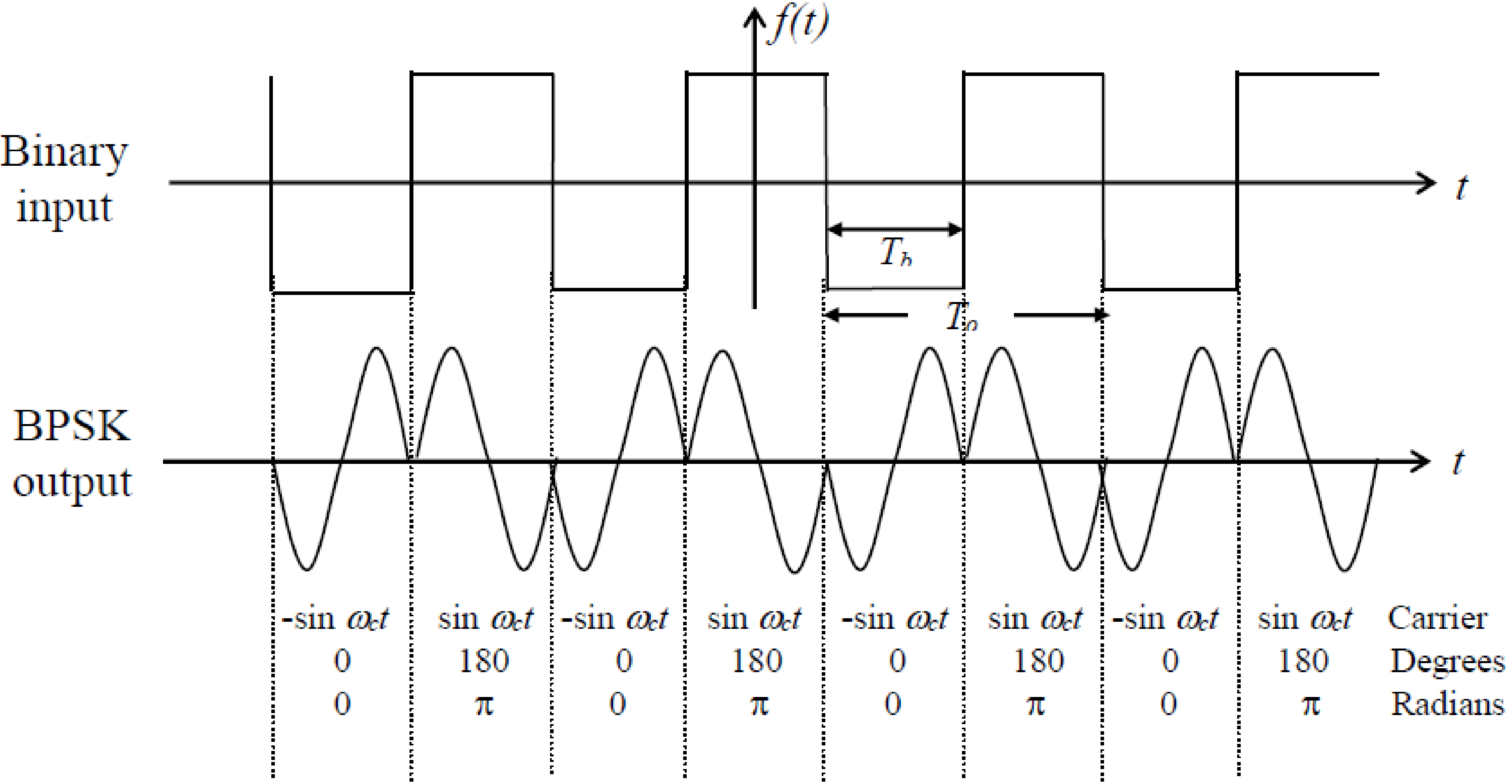


Fig.2.14 Output of BPSK Modulator

PSK Modulator

- Simplified block diagram of BPSK is shown in Fig.2.11
- Balanced modulator acts as a phase reversing switch.
- Carrier is transferred to output either in phase or 180^{o} with respect to reference carrier oscillator.
- Balanced ring modulator circuit is shown in Fig.2.12.
- Digital voltage must be much greater than the peak carrier voltage for proper operation.
  - For logic 1: D1 and D2 are ON while D3 and D4 are OFF, carrier voltage across T2 is in phase with the carrier voltage across T1 or the reference oscillator.
  - For logic 0: D1 and D2 are OFF while D3 and D4 are ON, carrier voltage across T2 is 180^{o} out of phase with reference oscillator.

Transmitter of BPSK

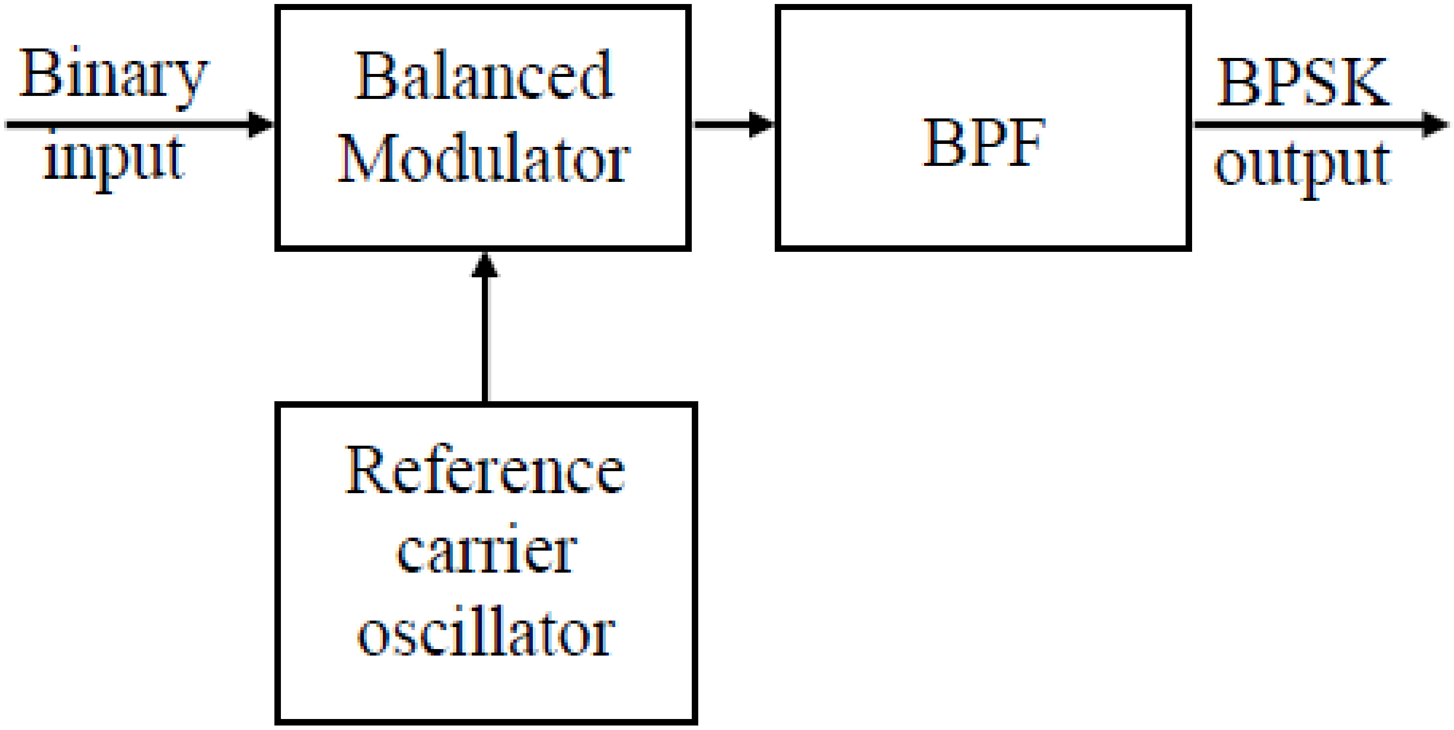


Fig.2.11 BPSK Modulator

PSK Balanced Ring Modulator

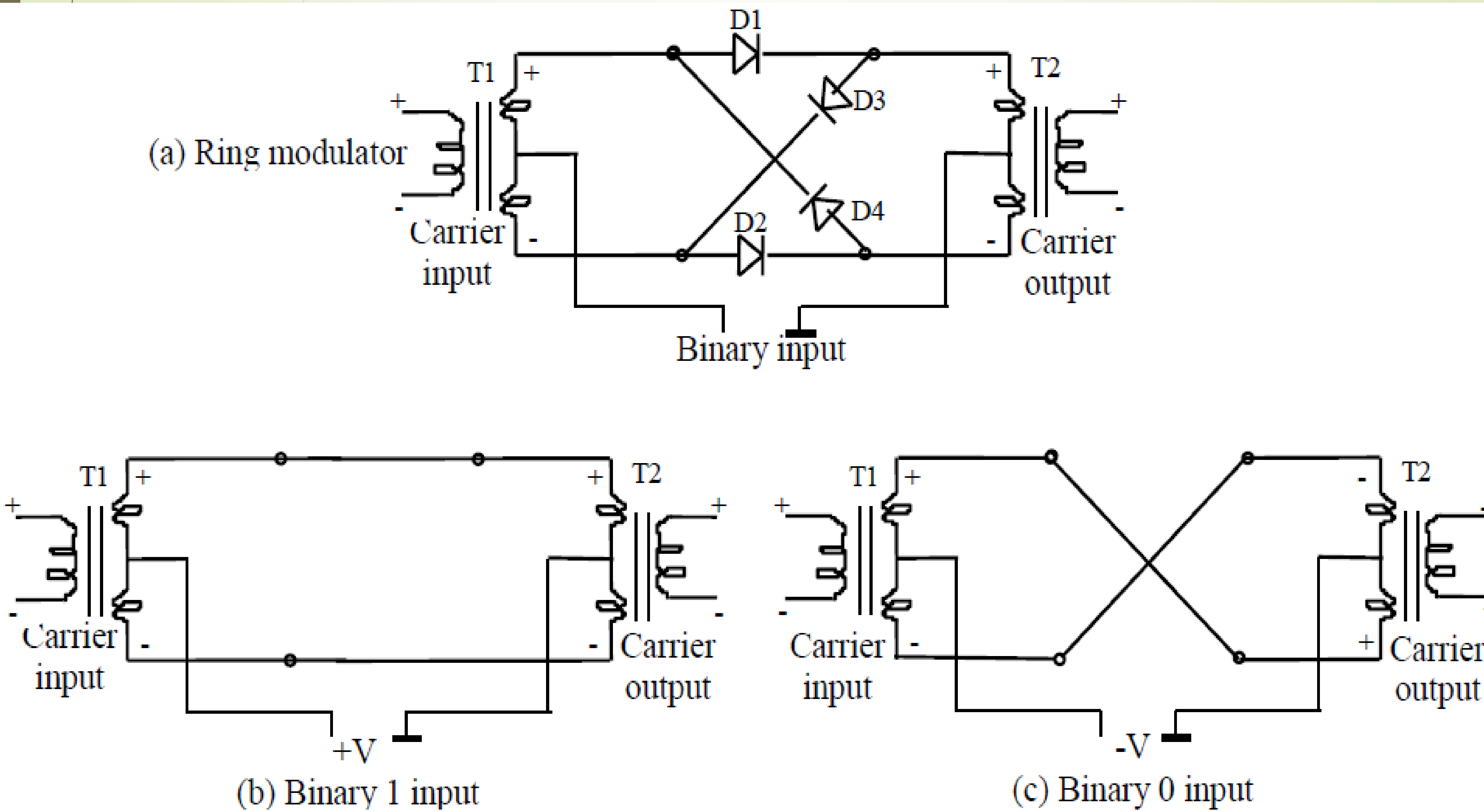


Fig.2.12 Balanced Ring Modulator

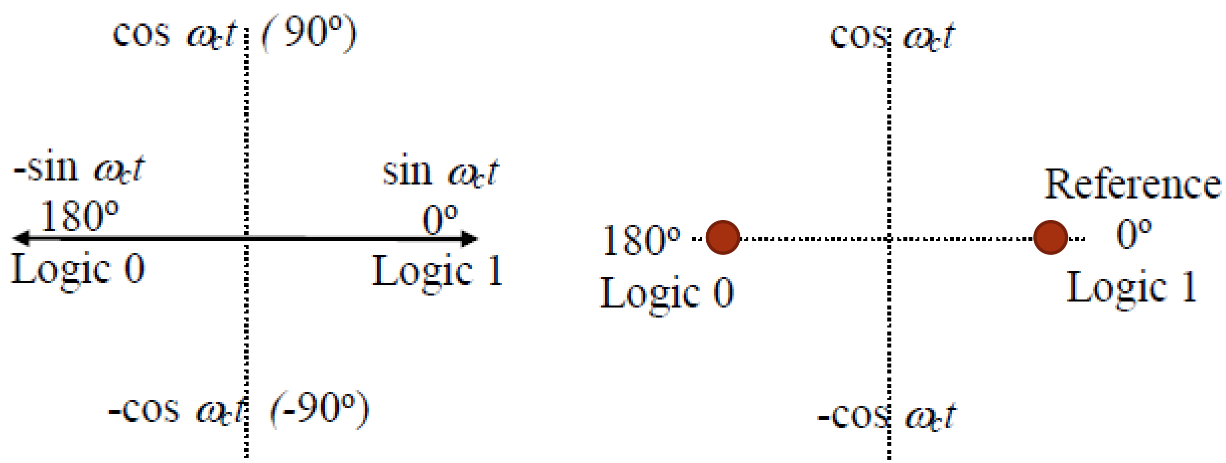
Representation of BPSK

- Figure shows truth table, phasor diagram and constellation diagram for a BPSK.
- Constellation diagram is similar to phasor except that the entire phasor is not drawn.
- Only the relative positions of the peaks of the phasors are shown.

Truth, Phasor, Constellation

Binary input	Output phase
Logic 0	180°
Logic 1	0°

(a) Truth table



(b) Phasor diagram

(c) Constellation diagram

Fig.2.13 BPSK Representation

Band Width of PSK

- Balanced modulator is product so carrier is multiplied by binary data (either +1 or –1).
- Also, widest bandwidth occurs when data is alternating 1/0 sequence.
- Product modulator output of the BPSK is:

$$output = \sin \omega_a t \sin \omega_c t = \frac{1}{2}\cos(\omega_c - \omega_a)t + \frac{1}{2}\cos(\omega_c + \omega_a)t$$

- Consequently, minimum double-sided Nyquist bandwidth is:

$$B_{BPSK} = (\omega_c + \omega_a) - (\omega_c - \omega_a) = 2\omega_a = 2(f_b / 2) = f_b$$

- Minimum bandwidth to pass worst-case BPSK equals input bit rate.

PSK Reception

- Simple block diagram of BPSK detection.

- Coherent carrier recovery circuit detects and regenerates carrier that is both frequency and phase coherent with the original transmit carrier.

- Balanced modulator output is the product of two inputs (BPSK signal and the recovered carrier).

- The LPF separates the recovered binary data from the complex demodulated spectrum.

Detection of BPSK

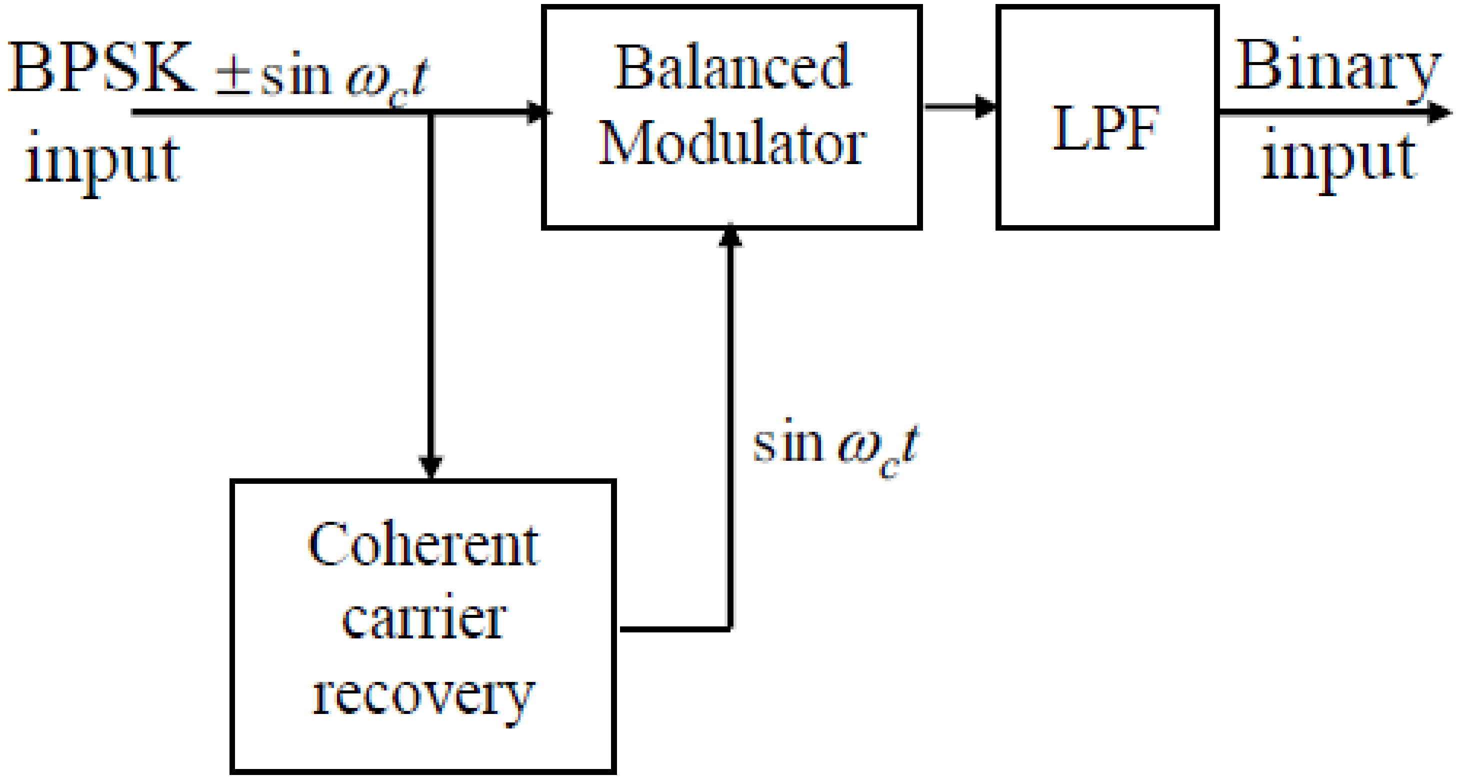


Fig.2.15 BPSK Receiver

Demodulation Process

- For input +*sin* $w_c t$ (logic 1), balanced output is:

$$Output = \sin\omega_c t \sin\omega_c t = \sin^2\omega_c t = \frac{1}{2}\left(1-\cos 2\omega_c t\right) = \frac{1}{2} - \frac{1}{2}\cos 2\omega_c t$$

$$Filter\ output = +\frac{1}{2} \quad dc\ voltage \equiv Logic\,1$$

- For input -*sin* $w_c t$ (logic 0), the output is:

$$Output = -\sin\omega_c t \sin\omega_c t = -\sin^2\omega_c t = -\frac{1}{2}\left(1-\cos 2\omega_c t\right) = -\frac{1}{2} + \frac{1}{2}\cos 2\omega_c t$$

$$Filter\ output = -\frac{1}{2} \quad dc\ voltage \equiv Logic\,0$$

M-ary Phase Shift Keying

M-ary Encoding

- In M-ary, one of M possible signals may be transmitted during each signaling interval.
- It is advantageous to encode at a level higher than binary, e.g., **4**PSK and **8**PSK.
- Each possible transmitted signal of an M-ary message sequence is referred to as "**symbol**".
- Mathematically, the number of bits per symbol n is related to the number of possible signals M by:

$$M = 2^n$$

-

Quadrature PSK

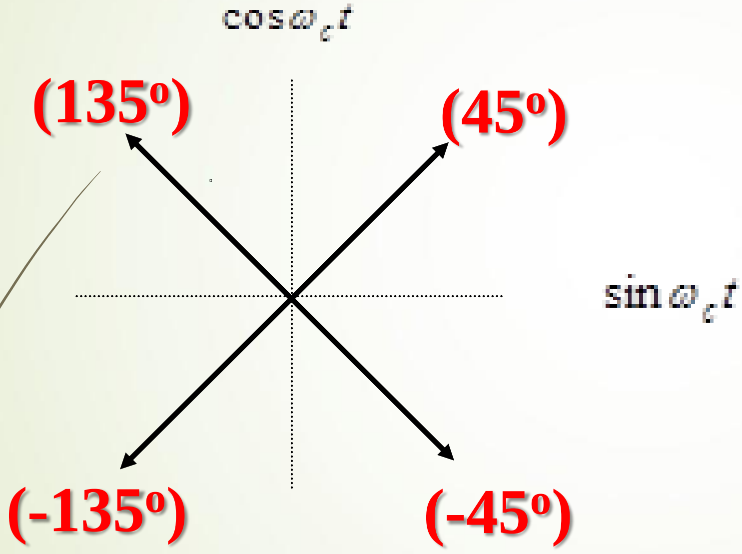
- QPSK, is another form of angle modulated, constant envelope digital modulation, and $M = 4$ possible symbols.
- 4 phases are possible for a single carrier frequency.
- Binary input data are combined into groups of 2 bits called dibits.
- Each dibit code generates one of the four possible output phases.
- For each 2- bit, a single output change occurs. So, the output baud rate is one-half of the input bit rate.
-

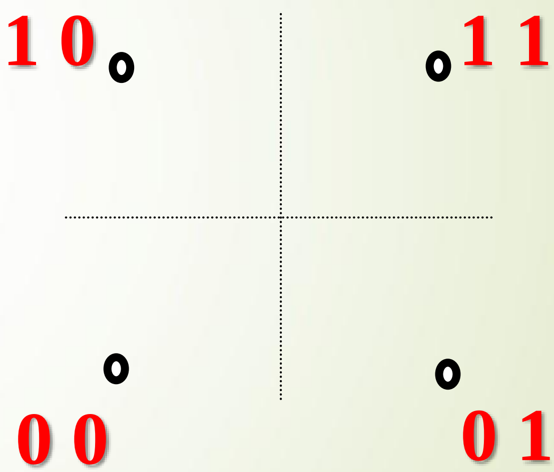
QPSK Truth Table

Inputs		Output
A	B	Phase
0	0	-135
0	1	-45
1	0	+135
1	1	+45

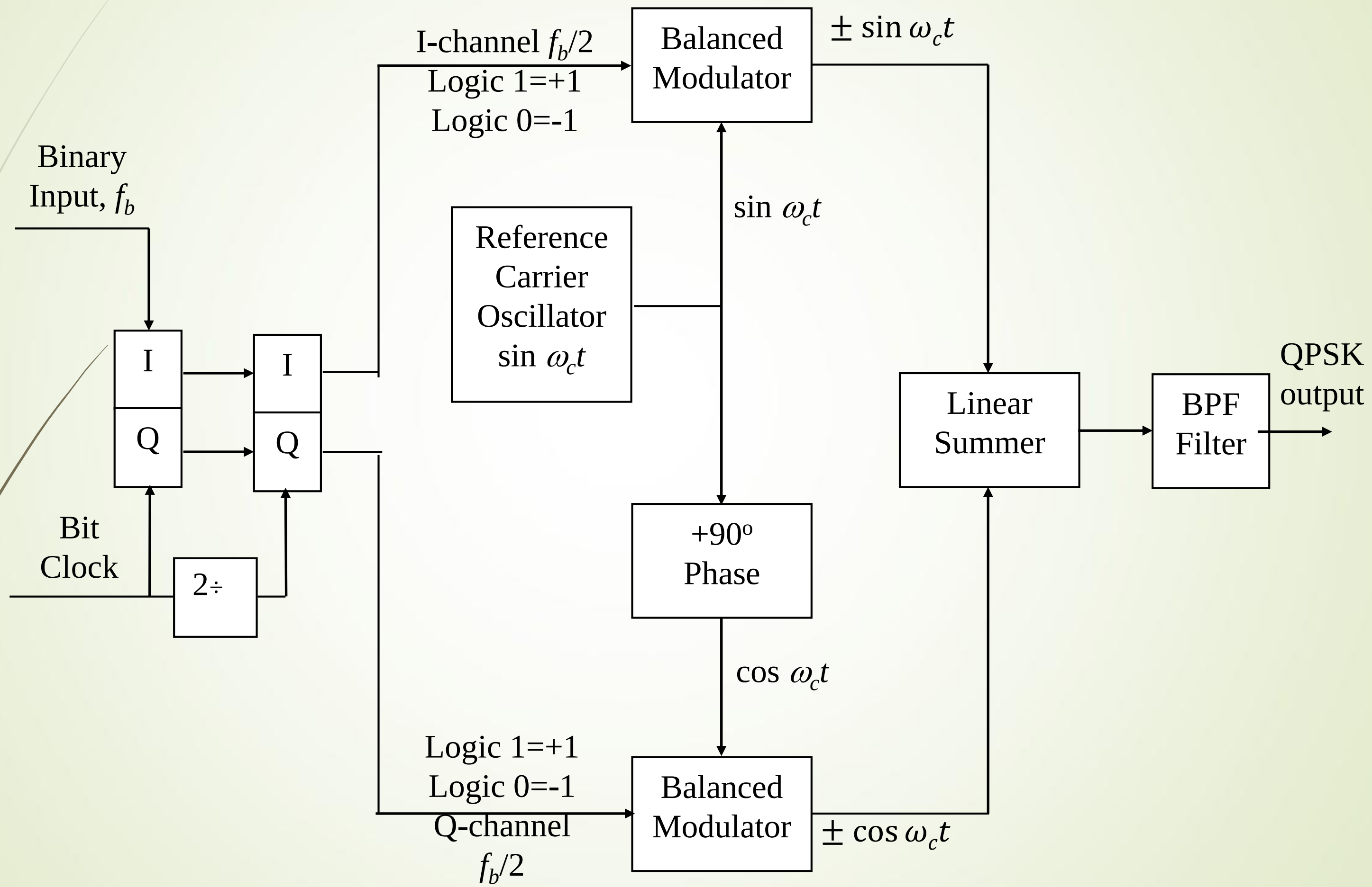
QPSK

Phasor Constellation





QPSK Transmitter



Transmitter Operation

- QPSK modulator is a two BPSK modulators combined in parallel.
- Two bits are clocked into the bit splitter.
- After both bits have been serially inputted, they are simultaneously parallel outputted.
- One bit is directed to I-channel to modulate the carrier that is in phase with the reference.
- Other bit is directed to Q-channel to modulate carrier that is 90^{o} out of phase or in quadrature with the reference.
- If linear summer combines the two quadrature signals, there are 4 possible phases as follows:

$$\pm \sin \omega_c t \pm \cos \omega_c t$$

Splitting to I and Q Channels

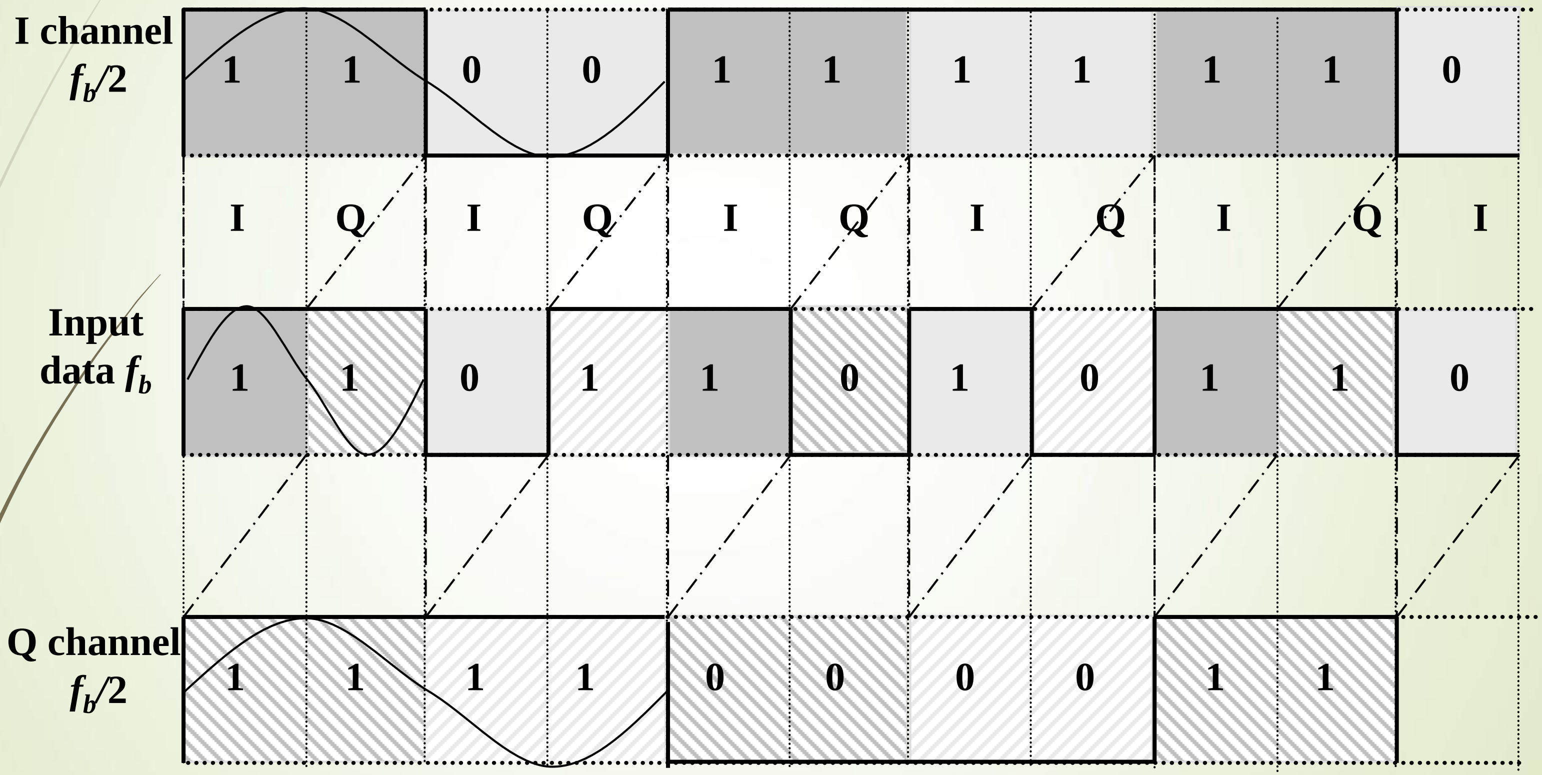


Fig.3.16: Highest Fundamental Frequency

Bandwidth of QPSK

- **Input data rate f_b is divided into two channels.**
- **I or Q channel bit rate is ½ input rate, i.e., $f_b/2$.**
- **Highest fundamental frequency at input of balanced modulators is one-fourth of input rate, i.e., $f_b/4$**
- **Balanced modulator product of I or Q channels:**

$$\boldsymbol{Output} = \sin\omega_a t \sin\omega_c t = \sin 2\pi\frac{f_b}{4}t \sin 2\pi f_c t$$

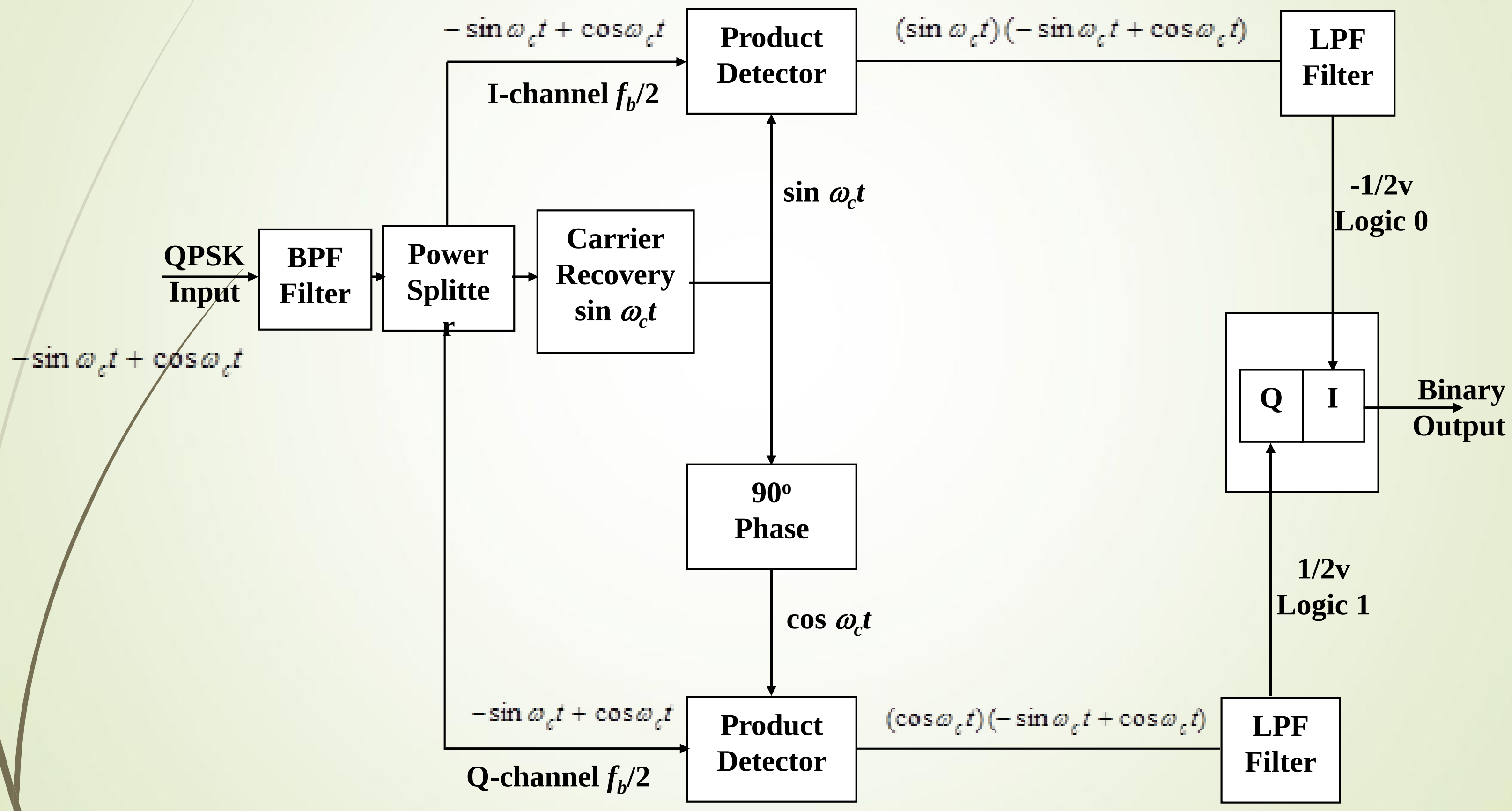
$$\boldsymbol{Output} = \sin 2\pi\left(f_c - \frac{f_b}{4}\right)t \sin 2\pi\left(f_c + \frac{f_b}{4}\right)t$$

- **So, output extends from fc-fb/4 up to fc+fb/4:**

$$\boldsymbol{BW_{QPSK}} = f_c + \frac{f_b}{4} - \left(f_c - \frac{f_b}{4}\right) = \frac{f_b}{2}$$

- **Minimum bandwidth of QPSK is less than incoming rate so that bandwidth is compressed to $f_b/2$ only.**

QPSK Receiver



Receiver Operation

- Power splitter directs QPSK signal into I and Q channels and carrier recovery circuit.
- Carrier recovery circuit reproduces the original transmit reference carrier.
- QPSK signal is demodulated in I and Q channels through product detectors.
- Detectors outputs are fed to combining circuit, to convert from parallel I and Q channels to a single binary output.

Offset QPSK [OQPSK]

A modified form of QPSK where the bit waveforms on I and Q channels are offset or shifted in phase by one-half of a bit time.

- It can be implemented by adding a delay.
- In QPSK, change from 00 to 11 or 01 to 10 causes 180° shift in output phase.
- Since changes in I channel of OQPSK occur at midpoints of Q bits, there is never more than a single bit change in the dibit code,
- So, 90° shift in phase improves performance.
- Disadvantage: changes in phase occur at twice the data rate so bandwidth is twice.

OQPSK Transmitter

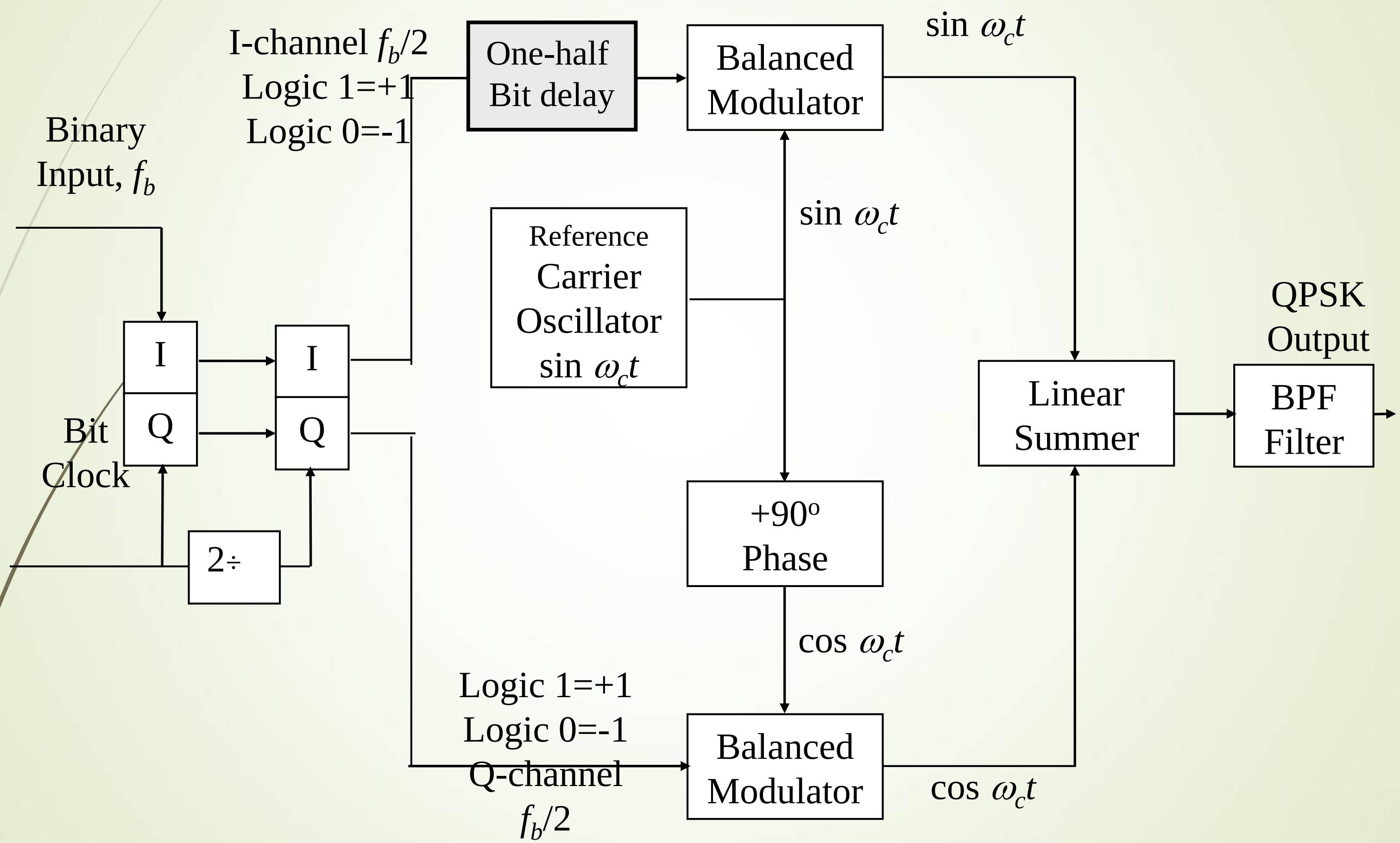
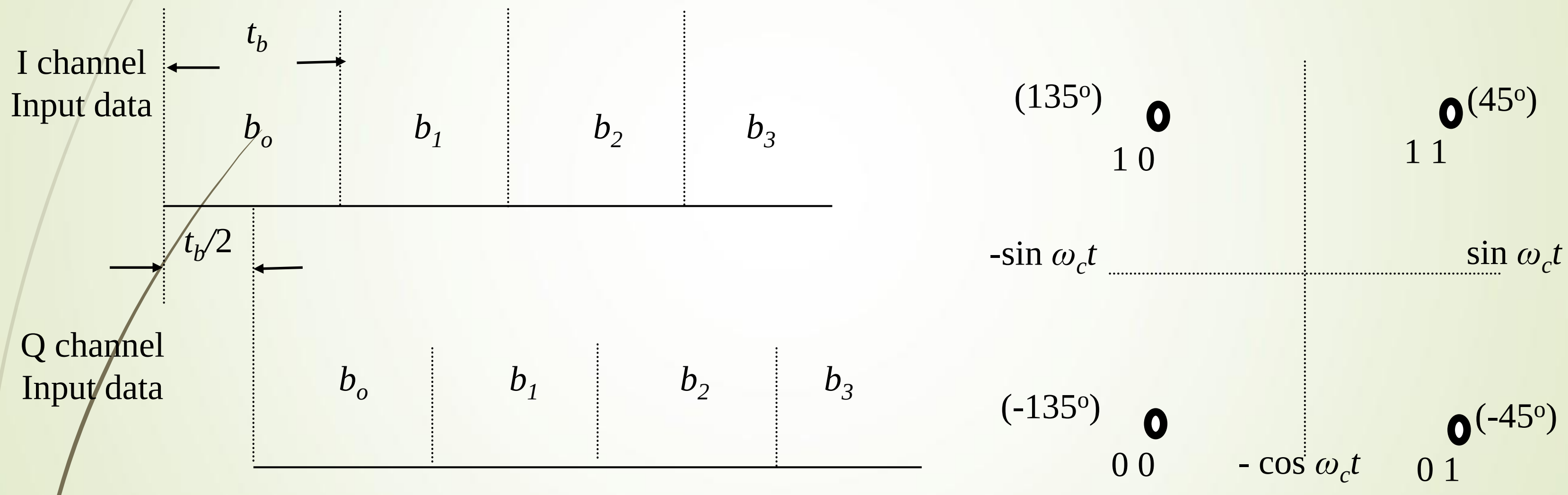


Fig.3.18: Offset QPSK Modulator

Offset Delay Concepts

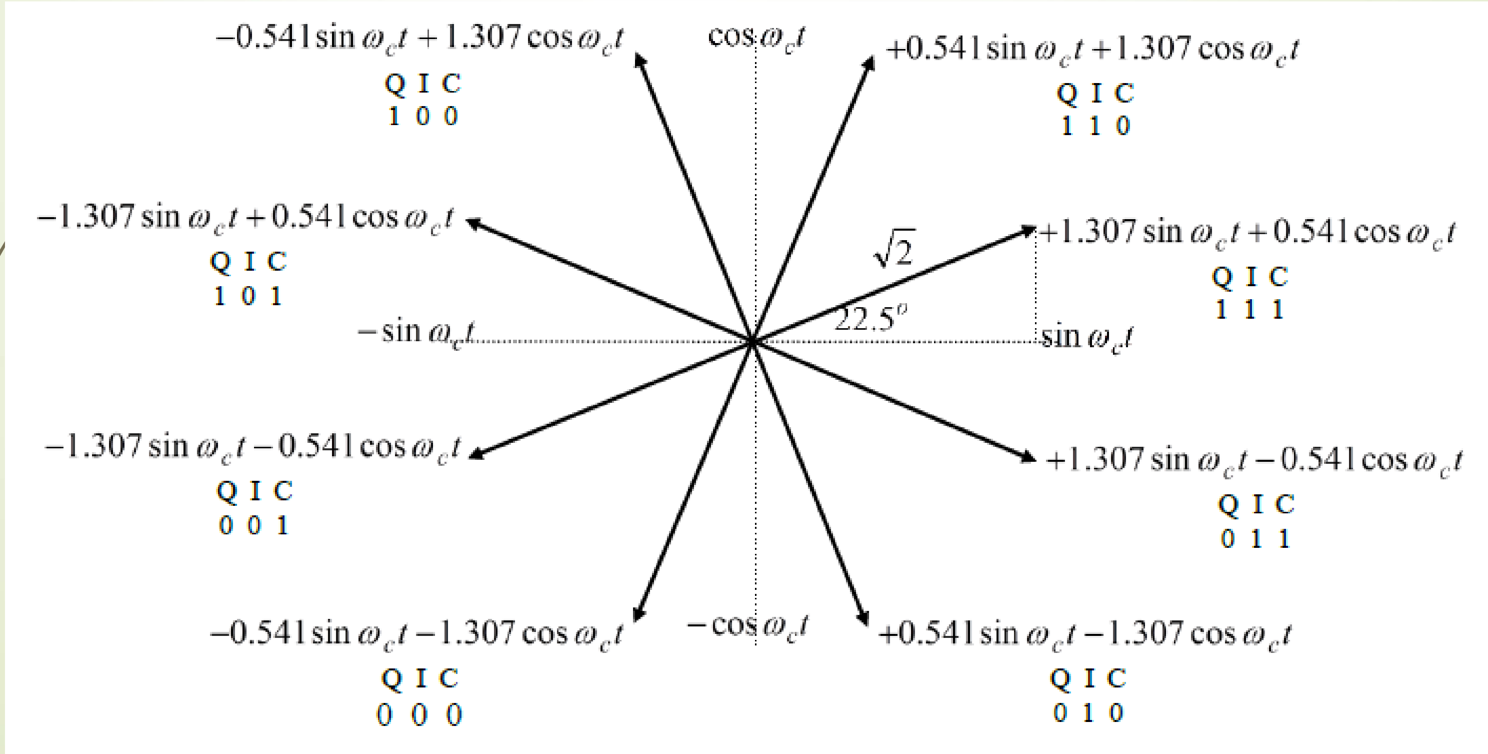


(a) Bit sequence alignment (b) Constellation diagram

Fig.3.19: OQPSK

8 PSK

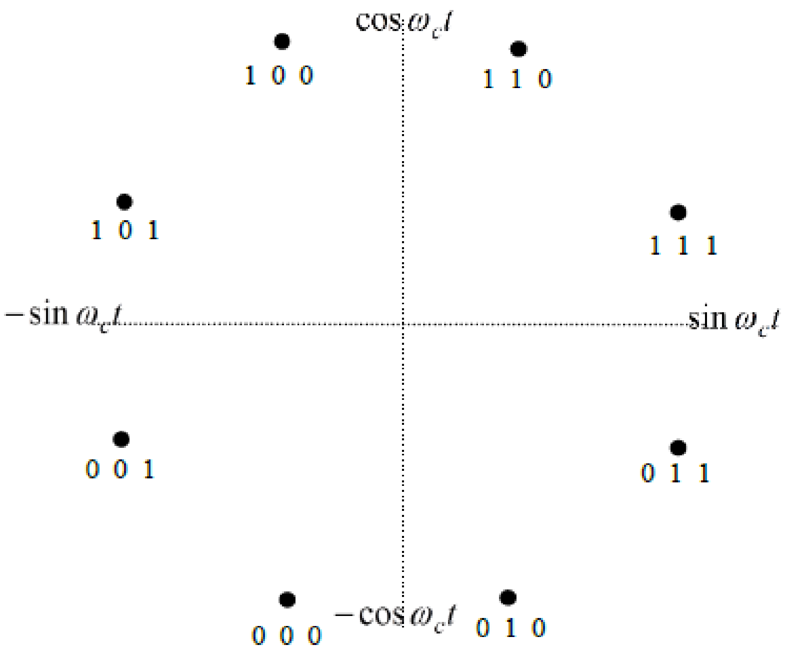
8PSK Phasor Diagram



8PSK
Truth - Constellation

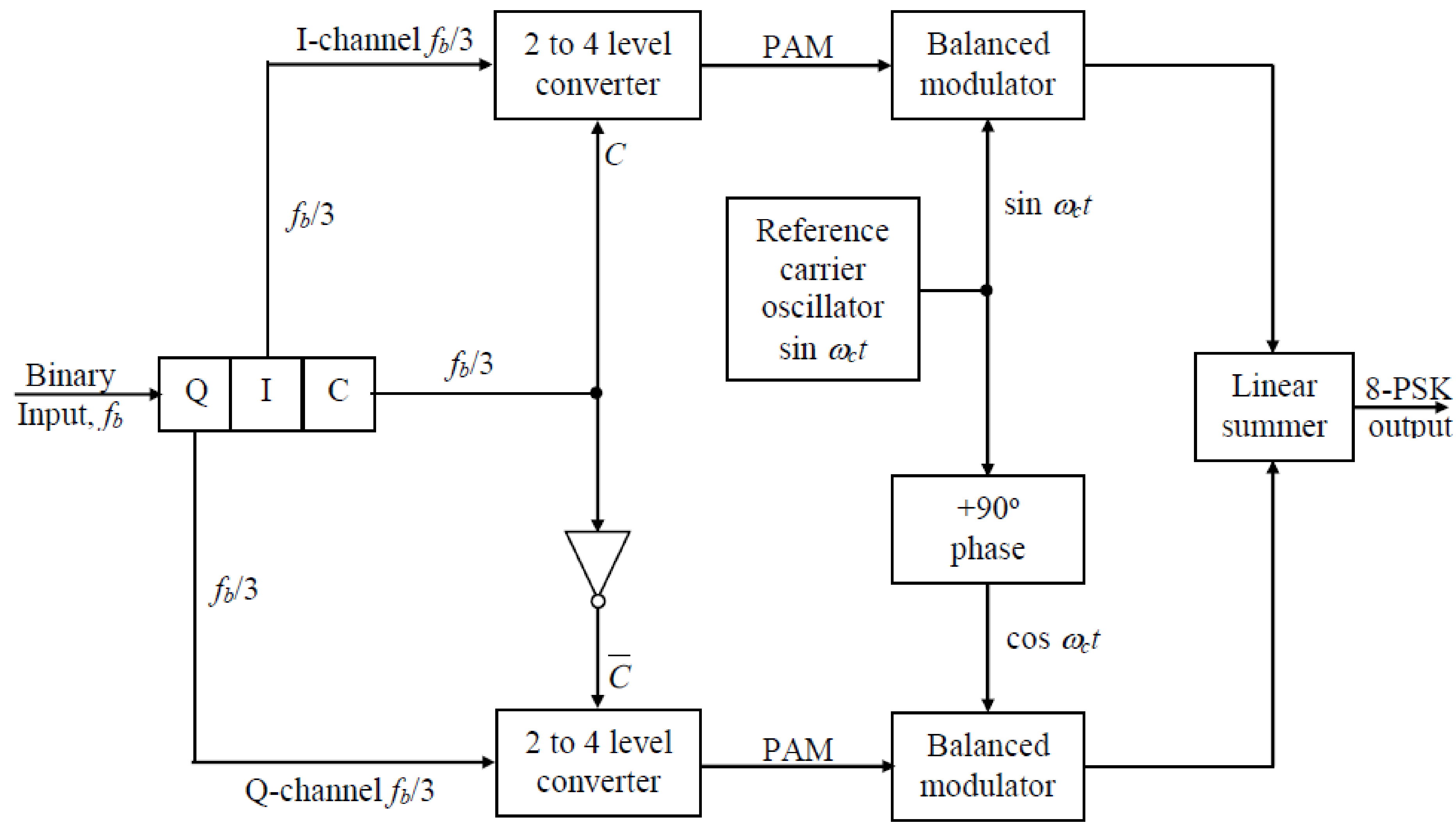
Binary input			8-PSK Output phase
Q	I	C	
0	0	0	-112.5
0	0	1	-157.5
0	1	0	-067.5
0	1	1	-022.5
1	0	0	+112.5
1	0	1	+157.5
1	1	0	+067.5
1	1	1	+022.5

(b) The Truth Table of 8-PSK



(c) Constellation diagram of 8-PSK

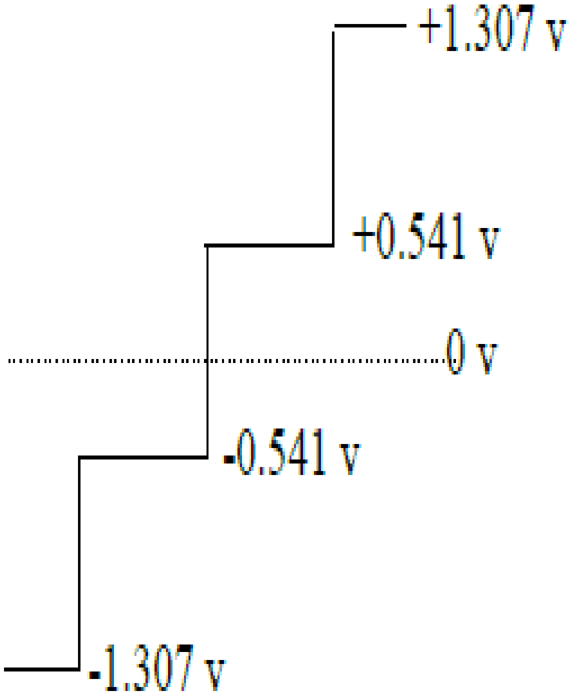
8PSK Transmitter



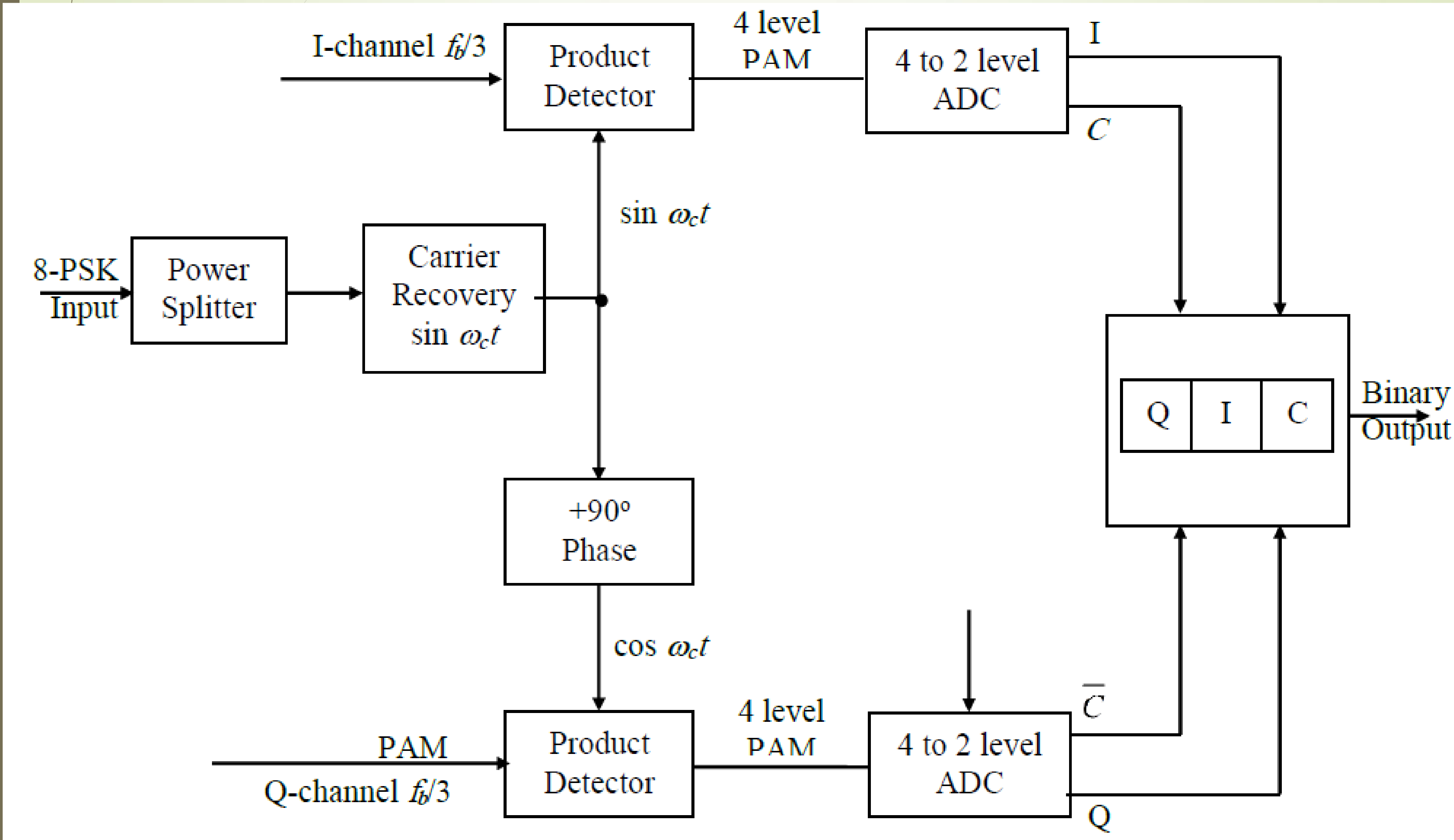
2-4 Levels Converter

I	c	Output
0	0	-0.541v
0	1	-1.307v
1	0	+0.541v
1	1	+1.307v

Q	$\bar{c}$	Output
0	1	-1.307v
0	0	-0.541v
1	1	+1.307v
1	0	+0.541v



8-PSK Receiver



QAM

Quadrature Amplitude Modulation

QAM

- QAM is a form of digital modulation, the information is contained in both the amplitude and the phase of the transmitted carrier.
- **8**-QAM is $\boldsymbol{M}$-ary encoding technique where $\boldsymbol{M} = 8$.
- **8**-QAM output is not a constant-amplitude signal such as **8**-PSK.
-

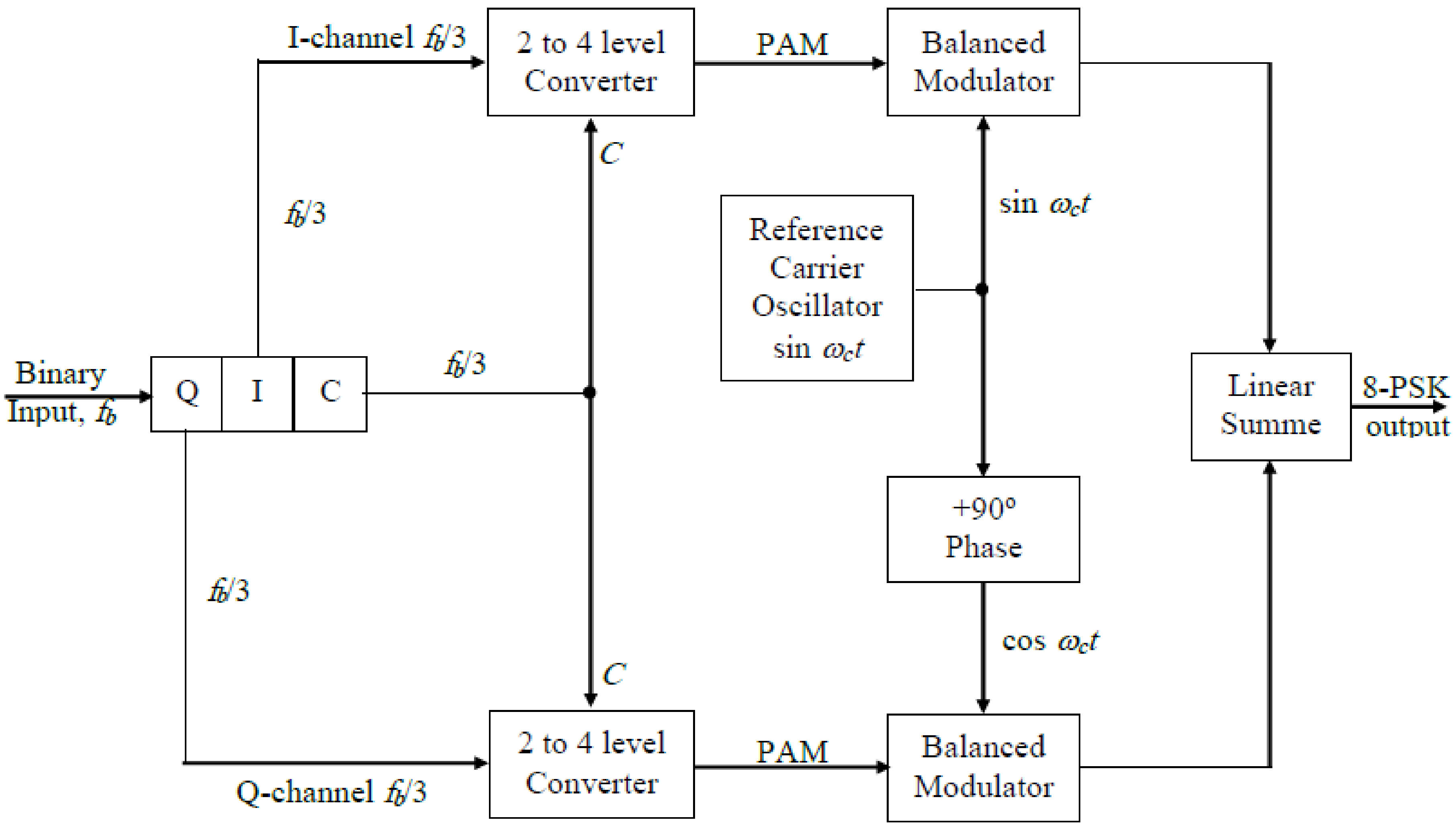
8-QAM Transmitter

- **8-QAM defers from 8-PSK in the inverter between the C and Q.**
- **Data are divided into I, Q, and C channels; each with a rate fb/3.**
- **I and Q bits determine the polarity of PAM signal at output of 2-to-4 level converters**
- **C channel determines the magnitude.**
- **8-QAM output is not a constant-amplitude signal such as 8-PSK.**

8-QAM Truth Table

BINARY INPUT			8-QAM OUTPUT	
Q	I	C	AMPLITUDE	PHASE
0	0	0	0.765 V	-135
0	0	1	1.848 V	-135
0	1	0	0.765 V	-45
0	1	1	1.848 V	-45
1	0	0	0.765 V	+135
1	0	1	1.848 V	+135
1	1	0	0.765 V	+45
1	1	1	1.848 V	+45

8-QAM Transmitter



Comparison

Table 2.2: Bandwidth Efficiency of Digital Modulation Techniques

Modulation	Encoding	Bandwidth, Hz	Baud rate	Efficiency, b/s/Hz
FSK	Single bit	$>f_b$	f_b	<1
BPSK	Single bit	f_b	f_b	1
QPSK	Di-bit	$f_b/2$	$f_b/2$	2
8-PSK	Tri-bit	$f_b/3$	$f_b/3$	3
8-QAM	Tri-bit	$f_b/3$	$f_b/3$	3
16-PSK	Quad-bit	$f_b/4$	$f_b/4$	4
16-QAM	Quad-bit	$f_b/4$	$f_b/4$	4

Squaring Loop

- The received BPSK signal is filtered to reduce the spectral width of noise.
- Squaring circuit removes the modulation and generates the second harmonic of carrier.
- This harmonic is phase tracked by PLL.
- The frequency of PLL (VCO output) is then divided by 2 and used as a phase reference for the product modulators.

BPSK Carrier Recovery

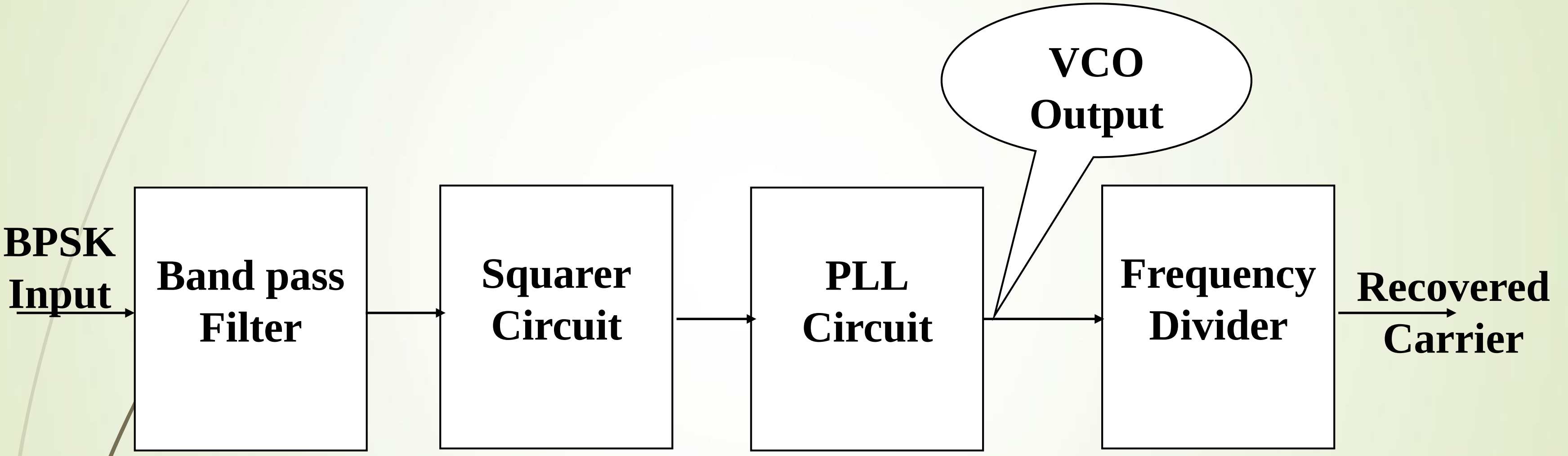


Fig.2.27 Squaring Loop Carrier Recovery for BPSK